

Question		Answer	Marks	Guidance
1	(i)	$\text{Mean} = \frac{59972}{40} = 1499$ <p>Condone full answer of 1499.3 (despite over-specification rule)</p> $S_{xx} = 96767028 - \frac{59972^2}{40} = 6851008$ $s = \sqrt{\frac{6851008}{39}} = \sqrt{175667} = 419$ <p>NB Full answer is 419. 1263 (but only allow to 4sf due to over-specification rule)</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>[3]</p>	<p>CAO Ignore units</p> <p>For S_{xx}</p> <p>CAO ignore units</p> <p>NB Allow 1500 NB Answer must be decimal M1 for $96767028 - 40 \times \text{their mean}^2$ BUT NOTE M0 if their $S_{xx} < 0$</p> <p>For s^2 of 176000 (or better) allow M1A0 with or without working For RMSD of 414 (or better) allow M1A0 provided working seen For RMSD² of 171000 (or better) allow M1A0 provided working seen For use of 1499: $S_{xx} = 6886988, s^2 = 176589, s = 420.225, \text{RMSD} = 414.9$ For use of 1500: $S_{xx} = 6767028, s^2 = 173513.5, s = 416.549, \text{RMSD} = 411.3$ Give same credit to answers as for correct answers</p>
1	(ii)	<p>New mean = $(0.163 \times 1499) + 14.5 = \text{£}258.84$ (No penalty for giving to 5sf as this is an exact sum of money)</p> <p>New sd = 0.163×419 = $\text{£}68.30$</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>[3]</p>	<p>If candidate 'starts again' only award marks for CAO Allow $\text{£}259$ or $\text{£}259.00$ from 1500 or $\text{£}258.89$ from 1499.3 Condone 258.8 and 258.9 Accept answers rounded to 3 sf or more eg $\text{£}258.80, \text{£}258.90$ Or for 0.163×419.1 oe</p> <p>Do not penalise lack of units in mean or sd Deduct at most 1 mark overall in whole question for over-specification of either mean or SD or both</p>

2	(i)	$P(X = 6) = 1 - P(X < 6) = 1 - \left(\frac{5}{6}\right)^3 = 1 - \frac{125}{216}$ $= \frac{91}{216}$	M1 M1 A1 [3]	For $\left(\frac{5}{6}\right)^3$ For $1 - \left(\frac{5}{6}\right)^3$ NB ANSWER GIVEN	
		OR: $= \left(\frac{1}{6}\right)^3 + 3 \times \left(\frac{5}{6}\right) \times \left(\frac{1}{6}\right)^2 + 3 \times \left(\frac{5}{6}\right)^2 \times \left(\frac{1}{6}\right)$ $= \frac{91}{216}$	M1 M1 A1	For second or third product term For attempt at three terms NB ANSWER GIVEN	Correct, including $\times 3$ or probabilities seen on correct tree diagram With no extras, but allow omission of $\times 3$ NB Zero for 1 – (sum of probs given in part (ii))
		OR: $= \frac{1 + 15 + 75}{216}$	M1 M1	for 15 or 75 seen	

			$= \frac{91}{216}$	A1	NB ANSWER GIVEN	
2	(ii)		$E(X) = \left(1 \times \frac{1}{216}\right) + \left(2 \times \frac{7}{216}\right) + \left(3 \times \frac{19}{216}\right) + \left(4 \times \frac{37}{216}\right) + \left(5 \times \frac{61}{216}\right) + \left(6 \times \frac{91}{216}\right)$ $= \frac{1071}{216} = \frac{119}{24} = 4.96 \text{ (exact answer 4.9583333)}$ $E(X^2) = \left(1 \times \frac{1}{216}\right) + \left(4 \times \frac{7}{216}\right) + \left(9 \times \frac{19}{216}\right) + \left(16 \times \frac{37}{216}\right) + \left(25 \times \frac{61}{216}\right) + \left(36 \times \frac{91}{216}\right)$ $= \frac{5593}{216} = 25.89$ $\text{Var}(X) = 25.89 - 4.958...^2$ <p>= 1.31 Accept answers in range 1.28 to 1.31 with correct working or 2261/1728 (Exact answer 1.308449...)</p>	A1 M1 A1 M1* M1* dep A1	<p>For Σrp (at least 3 terms correct)</p> <p>CAO</p> <p>For $\Sigma r^2 p$ (at least 3 terms correct)</p> <p>for – their $(E(X))^2$</p> <p>FT their $E(X)$ provided $\text{Var}(X) > 0$</p>	<p>Accept fractional answers Do not allow answer of 5 unless more accurate answer given first Use of $E(X-\mu)^2$ gets M1 for attempt at $(x-\mu)^2$ should see $(-3.96)^2, (-2.96)^2, (-1.96)^2, (-0.96)^2, 0.04^2, 1.04^2$, (if $E(X)$ wrong FT their $E(X)$) (all 6 correct for M1), then M1 for $\Sigma p(x-\mu)^2$ (at least 3 terms correct) Division by 6 or other spurious value at end and/or rooting final answer gives max M1A1M1M1A0, or M1A0M1M1A0 if $E(X)$ also divided by 6.</p> <p>Do not FT $E(X) = 5$ if full marks given for $E(X)$ Deduct at most 1 mark for over-specification of either mean or variance or both Unsupported correct answers get 5 marks (Probably from calculator)</p>
				[5]		

Question		Answer	Marks	Guidance												
3	(i)	$k + 0.01 + k + 0.04 + k + 0.09 + k + 0.16 + k + 0.25 = 1$ $5k + 0.55 = 1$ $k = 0.09$ <table border="1"> <tr> <td>r</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> </tr> <tr> <td>$P(X=r)$</td> <td>0.1</td> <td>0.13</td> <td>0.18</td> <td>0.25</td> <td>0.34</td> </tr> </table>	r	1	2	3	4	5	$P(X=r)$	0.1	0.13	0.18	0.25	0.34	M1 A1 B1 [3]	For equation in k NB Answer Given Complete correct table Allow substitution of $k = 0.09$ to show probabilities add to 1 with convincing working Must tabulate probabilities, though may be seen in part(ii)
r	1	2	3	4	5											
$P(X=r)$	0.1	0.13	0.18	0.25	0.34											
	(ii)	$E(X) = (1 \times 0.1) + (2 \times 0.13) + (3 \times 0.18) + (4 \times 0.25) + (5 \times 0.34)$ $= 3.6$ $E(X^2) =$ $(1 \times 0.1) + (4 \times 0.13) + (9 \times 0.18) + (16 \times 0.25) + (25 \times 0.34) = 14.74$ $\text{Var}(X) = 14.74 - 3.6^2$ $= 1.78$	M1 A1 M1* M1* dep A1 [5]	For $\sum rp$ (at least 3 terms correct Provided 5 reasonable probabilities seen. CAO For $\sum r^2 p$ (at least 3 terms correct) for – their $(E[X])^2$ FT their $E(X)$ provided $\text{Var}(X) > 0$ CAO If probs wrong but sum = 1 allow max M1A0M1M1A1. If sum $\neq 1$ allow max M1A0M1M0A0 (provided all probabilities ≥ 0 and < 1) No marks if all probs = 0.2 Use of $E(X-\mu)^2$ gets M1 for attempt at $(x-\mu)^2$ should see $(-2.6)^2, (-1.6)^2, (-0.6)^2, 0.4^2, 1.4^2$, (if $E(X)$ wrong FT their $E(X)$) (all 5 correct for M1), then M1 for $\sum p(x-\mu)^2$ (at least 3 terms correct with their probabilities) Division by 5 or other spurious value at end and/or rooting final answer gives max M1A1M1M1A0, or M1A0M1M1A0 if $E(X)$ also divided by 5. Unsupported correct answers get 5 marks (Probably from calculator)												

4	(i)	<table border="1"> <tr> <td>r</td> <td>2</td> <td></td> <td></td> <td></td> </tr> <tr> <td>$P(X=r)$</td> <td>k</td> <td>$8k$</td> <td>$15k$</td> <td>$24k$</td> </tr> </table> <p>$3k + 8k + 15k + 24k = 1$</p> <p>$k = 0.02$</p>	r	2				$P(X=r)$	k	$8k$	$15k$	$24k$	B1	For correct table (ito k or correct probabilities 0.06, 0.16, 0.30, 0.48)	For their four multiples of k added and =1. Allow M1A1 even if done in part (ii) – link part (ii) to part (i)
			r	2											
$P(X=r)$	k	$8k$	$15k$	$24k$											
M1	A1	or $k = 1/50$ (with or without working)													
			[3]												

4	(ii)	$E(X) = (2 \times 0.06) + (3 \times 0.16) + (4 \times 0.30) + (5 \times 0.48) = 4.2$ <p>or 21/5</p> $E(X^2) = (4 \times 0.06) + (9 \times 0.16) + (16 \times 0.30) + (25 \times 0.48) = 18.48$ $\text{Var}(X) = 18.48 - 4.2^2 = 0.84 = 21/25$	<p>M1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>[5]</p>	<p>For $\sum rp$ (at least 3 terms correct Provided 4 reasonable probabilities seen.</p> <p>cao</p> <p>For $\sum r^2 p$ (at least 3 terms correct)</p> <p>dep for – their $E(X)^2$</p> <p>FT their $E(X)$ provided $\text{Var}(X) > 0$ (and of course $E(X^2)$ is correct)</p>	<p>If probs wrong but sum = 1 allow full marks here. If sum $\neq 1$ allow max M1A0M1 M0A0 (provided all probabilities between 0 and 1)</p> <p>Or ito k NB $E(X) = 210k$, $E(X^2) = 924k$ gets M1A0M1M0A0. $E(X) = 210k$, $\text{Var}(X) = 924k - (210k)^2$ gets M1A0M1M1A0.</p> <p>Use of $E(X - \mu)^2$ gets M1 for attempt at $(x - \mu)^2$ should see $(-2.2)^2$, $(-1.2)^2$, $(-0.2)^2$, 0.8^2, (if $E(X)$ wrong FT their $E(X)$) (all 4 correct for M1), then M1 for $\sum p(x - \mu)^2$ (at least 3 terms correct with their probabilities)</p> <p>Division by 4 or other spurious value at end gives max M1A1M1M1A0, or M1A0M1M1A0 if $E(X)$ also divided by 4.</p> <p>Unsupported correct answers get 5 marks</p>
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5	(iv)	'Negative' or 'very slight negative'	E1 [1]	E0 for symmetrical but E1 for (very slight) negative skewness even if also mention symmetrical Ignore any reference to unimodal
	(v)	$E(X) = (0 \times 0.025) + (1 \times 0.1375) + (2 \times 0.3) + (3 \times 0.325) + (4 \times 0.175) + (5 \times 0.0375)$ $= 2.6$ $E(X^2) = (0 \times 0.025) + (1 \times 0.1375) + (4 \times 0.3) + (9 \times 0.325) + 16 \times 0.175 + (25 \times 0.0375) = 0 + 0.1375 + 1.2 + 2.925 + 2.8 + 0.9375 = 8$ $\text{Var}(X) = 8 - 2.6^2$ $= 1.24$	M1 A1 M1* M1* dep A1 [5]	For Σrp (at least 3 terms correct) CAO For $\Sigma r^2 p$ (at least 3 terms correct) for – their $E(X)^2$ FT their $E(X)$ provided $\text{Var}(X) > 0$ USE of $E(X - \mu)^2$ gets M1 for attempt at $(x - \mu)^2$ should see $(-2.6)^2, (-1.6)^2, (-0.6)^2, 0.4^2, 1.4^2, 2.4^2$ (if $E(X)$ correct but FT their $E(X)$) (all 5 correct for M1), then M1 for $\Sigma p(x - \mu)^2$ (at least 3 terms correct) Division by 5 or other spurious value at end gives max M1A1M1M1A0, or M1A0M1M1A0 if $E(X)$ also divided by 5. Unsupported correct answers get 5 marks.
	(vi)	$P(\text{Total of 3}) = (3 \times 0.325 \times 0.025^2) + (6 \times 0.3 \times 0.1375 \times 0.025) + 0.1375^3 = 3 \times 0.000203 + 6 \times 0.001031 + 0.002600 = 0.000609 + 0.006188 + 0.002600 = 0.00940$ $= (3 \times 13/64000 + 6 \times 33/32000 + 1331/512000)$	M1 M1 M1 A1 [4]	For decimal part of first term 0.325×0.025^2 For decimal part of second term $0.3 \times 0.1375 \times 0.025$ For third term – ignore extra coefficient All M marks above depend on triple probability products CAO: AWRT 0.0094. Allow 0.009 with working.